Freeway Performance Measurement System: Final Report

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FREEWAY PERFORMANCE MEASUREMENT SYSTEM:
Final Report of MOU 3012

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ABSTRACT

PeMS is a freeway performance measurement system for all of California. It processes 2 GB/day of 30-second loop detector data in real time to produce useful information. Managers at any time can have a uniform and comprehensive assessment of freeway performance. Traffic engineers can base their operational decisions on knowledge of the current state of the freeway network. Planners can determine whether congestion bottlenecks can be alleviated by improving operations or by minor capital improvements. Travelers can obtain the current shortest route and travel time estimates. Researchers can validate their theory and calibrate simulation models.

PeMS is a low-cost system. It uses the Caltrans network for data acquisition. It is easy to deploy and maintain. It takes under six weeks to bring a Caltrans district online. Functionality can be added incrementally. PeMS applications are accessed over the World Wide Web. Custom applications can work directly with the PeMS database. PeMS has been in stable operation for 18 months. Built as a prototype, PeMS can be transitioned into a 7x24 production system. The report describes the PeMS architecture and use.
INTRODUCTION

Caltrans (California Department of Transportation) needs a freeway performance measurement system that extracts information from real time and historical data. PeMS (Performance Measurement System) is such a system. It presents information in various forms to assist managers, traffic engineers, planners, freeway users, researchers, and value added resellers or VARs (VARs are businesses that package travel time information with other location-dependent services.)

PeMS obtains 30-second loop detector data in real time. Caltrans is divided into 12 districts; together they generate 2 gigabytes (GB) of data each day. District 7, Los Angeles, accounts for 1 GB. The PeMS database currently has 400 GB of data online.

PeMS is a low-cost system. It uses commercial-of-the-shelf products for communication and computation. Detector data are retrieved over the Caltrans ATM wide area network to which all districts are connected. The 45 Mbps link connecting PeMS to this network costs $2000/month. The PeMS computer is a four-processor SUN 450 workstation with 1GB of RAM and 1 terabyte of disk. It uses a standard Oracle database for storage and retrieval.

The PeMS software architecture is modular and open. A new district can be added online with six person-weeks of effort, with no disruption of the district’s TMC (Traffic Management Center). Data from new loops can be incorporated as they are deployed. New applications are added as need arises. PeMS has been in stable operation for 18 months. Although it is a prototype, it can serve as the blueprint for a 7x24 production system. A copy of PeMS would cost less than $300,000. A part-time database administrator maintains PeMS.

PeMS is easy to use; built-in applications are accessed through a Web browser. Custom applications can work directly with the database. PeMS brings large benefits. Caltrans managers can instantaneously obtain a uniform, and comprehensive assessment of the performance of their freeways. Traffic engineers can base their operational decisions on knowledge of the current state of the freeway network. Planners can determine whether congestion bottlenecks can be alleviated by improving operations or by minor capital improvements. Traffic control equipment (ramp-metering and changeable message signs) can be optimally placed and evaluated. Travelers can obtain the current shortest route and travel time estimates. PeMS can serve to guide and assess deployment of intelligent transportation systems (ITS).

The remainder of the report is organized as follows. The next section summarizes the communication and software architecture. The following section describes PeMS applications. The last section collects some concluding observations. The Appendix consists of an empirical study of congestion, capacity, and ramp metering using PeMS.
PEMS ARCHITECTURE

Figure 1 shows the communication architecture. The PeMS computer, *transacct*, is located in the University of California at Berkeley. Users access PeMS over the Internet. *Transacct* also has a 45 Mbps link to the Caltrans ATM wide area network (WAN). The WAN is used to transfer data from districts to PeMS.

An individual Caltrans district is connected to PeMS over a permanent ATM virtual circuit. To establish such a circuit the routing tables at the two ends must be configured. The configuration is done remotely from Caltrans Headquarters in Sacramento.

A district TMC and PeMS collect data as follows. A “front end processor (FEP)” at the TMC receives data from freeway loops every 30 seconds. The FEP formats these data and writes them into the TMC database as well as into the PeMS database.

PeMS maintains a separate instance of the database for each district. Although the table formats vary slightly across districts, they are stored in PeMS in a uniform way, so the same software works for all districts.

The software is organized in three layers. At the bottom is database administration. The work is standard but highly specialized: disk management, crash recovery, table configuration. Many parameters must be tuned to improve database performance. A part-time Oracle database administrator is necessary.

The top layer comprises applications that are described in the next section. The middle layer comprises software that works on the data as they arrive in real time. It

- Aggregates 30-second values of flow and occupancy to lane-by-lane, 5-minute values;
- Calculates the $g$-factor of each loop;
- Uses the g-factor to calculate the speed for each lane;
- Aggregates the lane-by-lane value of flow, occupancy, and speed across all lanes at each detector station. At this point, PeMS has flow, occupancy, speed, and travel time for each 5-minute interval for each detector station (one station typically serves the detectors in all the lanes at one location);
- Computes the basic performance measures.

Most detectors in California have single loops that report two numbers every 30 seconds: *flow* or the number of vehicles that crossed the loop, and *occupancy* or the average fraction of time a vehicle is present over the loop. The formula to calculate speed is

$$speed = g \times \frac{flow}{occupancy}.$$ 

The “$g$-factor” depends on both the actual vehicle length, which varies by lane and over the course of a day, and the loop’s electrical circuit, which varies randomly across loops.
Districts typically assume a constant value of $g$. The assumption leads to errors in speed estimates of 100 percent or more. PeMS uses an adaptive algorithm that tracks the $g$-factor of each loop separately to provide accurate speed estimates.

The 5-minute averages concern individual links. A *link* is a section of freeway that holds a single loop detector. PeMS computes these performance measures for each link: delay, VMT, VHT, and travel time. *Delay* ($d$) over a link during a 5-minute interval is

$$d = length \times flow \times \left[ \frac{1}{speed} - \frac{1}{V} \right].$$

Here *length* is link length. (In California, detectors are placed one-third to one-half mile apart.) $V$ is the target speed (35 mph in California). Speed below $V$ is considered congestion, so delay is the additional vehicle-hours spent due to congestion. (In the formula above, $x^+ = \max(x, 0)$.

$$VMT = flow \times length, \quad VHT = \frac{VMT}{speed}, \quad \text{and } Q = \frac{VMT}{VHT}.$$  

$VHT$ is the number of vehicle-hours spent by travelers (over a five-minute interval) on that link, and $VMT$ is the number of vehicle-miles they have traversed. Thus $VHT$ is the input of the link (vehicle-hours per 5 minutes) and $VMT$ is the link output (vehicle-miles per 5 minutes). The ratio, $Q = \frac{VMT}{VHT}$, is the vehicle-miles-weighted speed or *productivity* of the link during a single 5-minute interval. (See Figure 2).

Observe that it makes sense to add up $VMT$ and $VHT$ over any set of links (for example, one freeway) and time periods (for example, one day). The ratio, $Q$, is the productivity of that freeway on that day. Comparing $Q$ over different days, or on the same day in different weeks, gives a quick summary of changes in freeway performance. Lastly, the *Travel Time* over a link starting at the beginning of a 5-minute interval is

$$Travel\ Time = \frac{length}{speed}.$$  

Here *length* is length of a link and *speed* is the estimated speed. The travel time over a route is estimated by adding the travel times over the links constituting the route. (More sophisticated estimates are being investigated.)

**USES OF PEMs**

Users run various applications through their Web browsers. Authorized users may directly query the database and develop custom applications. The following scenarios illustrate the use of PeMS by transportation managers, traffic engineers, travelers, VARs, and researchers.
Managers

It is a truism that “If you can’t tell how your system performed yesterday, you can’t expect to manage it today.” A manager pulls up PeMS on her Web browser to compare the performance of her district’s freeways with previous days. Figure 2 displays the daily productivity, \( Q \), for the 23-mile northbound direction of I-405 freeway (405N) in District 12, Orange County, for the period 5/1/98 to 5/20/98. The manager observes that on 5/8/98 and 5/12/98, the average vehicle-mile-weighted speed or \( Q \) fell below 30 mph. She could initiate an inquiry whenever \( Q \) fell below, say, 30 mph. She also could compare the performance of other freeways in her district, and allocate resources towards improving the worst performers.

Engineer

In response to the manager’s inquiry, the engineer asks PeMS to display a contour plot of speed for the 24-hour period of 5/12/98 over the 23-miles of 405N. From that plot, which is too intricate to reproduce well here, the engineer observes four areas of congestion. Two of these occur in the morning and two in the evening commute hours. Figure 3 shows one of these, a 4-mile stretch from post mile 1 to 5, beginning at 6.30 am and ending at 9.30 am. Looking at plots of other days, the engineer verifies that all four are areas of recurrent congestion, although 5/12/98 is worse than usual. The plot of Figure 3 near post mile 1 is anomalous. Contour plots on other days at the same location reveals the same anomaly. The engineer uses PeMS to verify that the loop detectors at this location are not working properly. He sends a request to the loop maintenance crew to investigate the detector station.

PeMS creates a map of the entire freeway network for each 5-minute interval in which each link is colored according to speed or any of the other computed averages (see Figure 4). An “animation” application plays back these maps in sequence over any time interval. The engineer can use this application to visualize the behavior of the network on 5/12/98. The animation makes vivid how congestion starts and spreads. (New staff members can use the animation to quickly get a “feel” for the district’s traffic patterns.)

Traveler

TV and radio reports of freeway conditions are spotty (“there is a three-car accident on 405N at Edwards”). You can’t use the reports to estimate the shortest travel time and route for your trip. No one today provides such travel time estimates and shortest routes. PeMS provides these. You bring up the district freeway map on your Web browser, and select an origin and destination. PeMS decorates the map with two shortest routes, depending on whether or not you can use the High Occupancy Vehicle (HOV) lanes, and a caption containing the corresponding travel times. Figure 4 is an example. In this instance, the caption states that the HOV route in Figure 4 is 23.0 miles long and takes 22 minutes. The non-HOV route is also 23.0 miles long but it takes 59 minutes.

Often you want to know the travel time you would face, say, 30 minutes from now. The upper chart of Figure 5 is the empirical distribution of travel times over the 23-mile stretch of 405N for trips that started at 8:30 am on any Tuesday of 1998. This distribution says that with 90 percent probability you will reach your destination within 50 minutes. However, if you know that a trip that started at 8.00 took less than 27.5 minutes, you can reduce the...
prediction to 40 minutes (middle chart). But, if you know that the earlier trip took more than 37.5 minutes, you should plan on taking 55 minutes (lower chart). Thus appropriately combining historical and current trip times reduces uncertainty in future trip time.

VARs—Value Added Resellers (Travel Information Service Providers)

If you were stuck on a freeway, you would want to know how long your trip will take, whether you should call in late for your appointment, or cancel it altogether. You could one day access PeMS with your cell phone to find out. A VAR that provides this service could also send you alerts during your trip if the traffic situation changed so that your trip will take, say, 20 minutes longer than was estimated when you began your trip. PeMS has developed such a prototype for a Web-enabled cell phone.

Planner/Researcher

Congestion imposes a burden on many Californians. Reliable estimates are not available, but the monetary value of time wasted in congestion is surely in the millions of dollars each day. The state cannot afford to build additional freeways to relieve congestion. It must improve the productivity of its freeways through the use of Information Technology (IT). The most important question to answer is: By how much can IT reduce congestion PeMS can help answer this question.

Congestion may be measured by Caltrans’ definition of Delay, or by using VHT and VMT. For a particular freeway call this Delay_total. Traffic theory allows us to decompose the delay in two parts:

\[
\text{Delay}_{\text{total}} = \text{Delay}_{\text{congestion}} + \text{Delay}_{\text{demand}}.
\]

The first component, Delay_congestion, is the result of congestion that reduces freeway throughput to less than capacity. In principle, this delay can be completely eliminated by ramp-metering that maintains throughput at the freeway capacity. Assume this is done. There remains the second component, Delay_demand. This is caused by travel demand in excess of freeway capacity. Only demand shifting can reduce that delay. One way to shift demand is to use PeMS to inform travelers that they will face this delay. Travelers that are better off changing their trip origination time (or travel mode) would then do so.

We can use PeMS to analyze delay for any section of freeway. Figures 6 and 7 summarize the analysis of a 6.3-mile stretch of 405N from 5.00 to 10.00 am on 6/1/98. Figure 6 plots VMT vs. VHT. Each point is a pair of numbers (VHT, VMT) corresponding to a five-minute interval. VHT is the number of vehicle-hours spent per five minutes during a particular 5-minute interval and VMT is the vehicle-miles traveled per five minutes in the same interval. In the figure VHT is expressed in vehicle-hours per hour and VMT in vehicle-miles per hour. There are 60 points in all for the five-hour interval; the points corresponding to 7.15, 7.30, 8.00, 8.30 and 9.00 are marked. At 5.00 am VHT= 160 and VMT = 10000, corresponding to an average speed of 62.5 mph. Average speed remains constant while the throughput measured in VMT increases until 7.15 am when the VMT reaches its maximum value of 58000. (This arguably should be called the capacity of this stretch of freeway.)
From 7.15 to 7.30, VMT remains at capacity but VHT increases by 20 percent from 1000 to 1200. So the density on the freeway has increased and the speed has dropped by 20 percent: queues are building up on the freeway. Between 7.30 and 8.00 flow has collapsed; VMT is 48000 (16 percent below capacity), and VHT has increased to 1550, giving an average speed of 30 mph. The situation recovers one hour later at 9.00 am. At that time VMT is well below capacity indicating that demand has to drop significantly below capacity before speed recovers.

With PeMS you could observe this congestion develop in real time. Appropriate ramp-metering strategy would throttle the inflow at the beginning of the congestion period (when throughput reaches capacity, at 7.15 am in this case). In principle, the reduction in throughput, and the corresponding Delay_congestion could be eliminated.

The uppermost plot in Figure 7 is the actual VHT per 5 minutes on this section from 5 am to 10 am. The middle plot gives the VHT the same vehicles would spend if perfect metering maintained throughput at capacity. The lowest plot is the VHT that would result if demand-shift eliminated queues at ramps. The area between the topmost and middle curves is the first component, Delay_congestion; the area between the middle and lowest curve is Delay_demand. So the area between the topmost and lowest curves is Delay_total. An inspection of Figure 6 suggests that for this example Delay_congestion ≈ 500 vehicle-hours and Delay_demand ≈ 200 vehicle-hours.

CONCLUSIONS

California’s citizens and businesses face increased freeway congestion. The cost in time, money, stress, and pollution is large. Caltrans is planning to deploy ITS technology to relieve congestion. But these plans are debated, revised, and launched in analytical darkness. No one knows how well the freeways are operated, what targets for operations improvement are realistic, and how those targets might be achieved.

For example, Caltrans publishes congestion measures of daily vehicle-hours of delay. To estimate this delay, cars equipped with computers that record speed and distance are driven along each section of congested freeways, during commute periods, twice a year. A glance at Figure 2 shows there is a huge daily variation in delay, so that congestion measured this way is a random number. It is unsurprising that Caltrans does not use these estimates to formulate congestion reduction goals or to guide capital improvements.

Caltrans is evolving a strategy for ITS deployment, founded on a performance evaluation system. This system would help managers, planners, and engineers accurately estimate current performance; discover locations where improvements are likely to be most effective; evaluate in advance the benefits of suggested investments (ramp-metering, changeable message signs, freeway service polls, etc); and, after those investments are made, measure the resulting benefits. Such a system should be part of the daily operations, just as production, cost, sales and revenue figures are essential in the daily operations of a private corporation. PeMS can be a key element of the Caltrans performance evaluation system.
ACKNOWLEDGEMENTS

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<tr>
<td></td>
<td></td>
<td><strong>22 min</strong> using HOV lanes</td>
<td>23.0 miles (HOV)</td>
</tr>
</tbody>
</table>
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Appendix: Congestion, excess demand, and revealed capacity in California freeways

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Abstract

The paper makes four assertions, supported by an extensive empirical study of freeways in Los Angeles and Orange County. First, maximum throughput occurs at the free flow speed of 60 mph, and not between 35 and 45 mph, as is often assumed. So congestion must be measured as the additional vehicle-hours of delay traveling below 60 mph.

Second, the maximum throughput over a link depends on how a link is connected to other links and the pattern of traffic, as well as its physical characteristics. A challenge to traffic theory is to determine the maximum throughput of a link, given the network topology and traffic pattern.

Third, the congestion delay can be divided into (1) the portion that can be eliminated by ramp metering, and (2) the delay due to excess demand. There is a systematic procedure to calculate these two components of delay for recurrent congestion, using loop-detector data. The procedure is illustrated for a 6-mile stretch of I-405N in Orange County on June 1, 1998, 5.00-10.00 am.

Fourth, recurrent congestion evolves over three phases: increased demand is first met at free flow speeds, until the demand exceeds maximum throughput and congestion starts; both flow and speed then decrease and occupancy increases; only after demand drops well below maximum throughput does occupancy decrease and speed increase until free flow is reestablished. So the objective of ramp metering must be to maintain free flow and maximum throughput. It is a challenge to design such a ramp metering algorithm.

1 Introduction

There is interest within the California Department of Transportation or Caltrans in measuring freeway congestion, setting realistic congestion-reduction targets, and making appropriate investments.
to meet those targets. But opinions differ over how to measure congestion; how much congestion can be eliminated by metering and how much of it is due to excess demand, requiring demand management for its reduction; and the relative magnitudes of recurrent vs non-recurrent congestion. The reason for these differences is simple: in the absence of reliable empirical knowledge of congestion and its causes, people holding different opinions won’t change them. This paper summarizes evidence to resolve some of these differences. It is a report of the PeMS (Performance Measurement System) project—a large-scale study to measure the performance of California freeways [2].

Congestion measures compare the actual travel time to some standard. There are two defensible standards: one is travel time under free flow conditions, the other is travel time under maximum throughput. We demonstrate that in California, the two standards coincide: maximum throughput occurs at the free flow speed of 60 mph. So the standard proposed here is to measure congestion as the additional vehicles hours spent traveling below 60 mph. Caltrans today declares a link congested if its speed is below 35 mph for at least 15 min. This practice cannot be justified and should be replaced by 60 mph.

We call the maximum observed sustainable throughput in a link its revealed capacity. It is generally quite different from the Highway Capacity Manual’s definition of capacity which is a function of the link’s physical characteristics. Revealed capacity depends on how a link is interconnected with other links, the pattern of demand, and its physical characteristics. Revealed capacity is an empirical notion—it is the maximum observed throughput over a link during recurrent congestion. The fact that this maximum throughput is remarkably stable, despite daily fluctuations, suggests that the notion reflects some more stable phenomenon. It is a challenge to theoretically explain revealed capacity.

Congestion can be reduced or eliminated by proper ramp-metering and by demand diversion. Put inversely: imperfect metering and excess demand cause congestion. The PeMS procedure provides a theoretically sound way to divide congestion between these two causes. Moreover, numerical calculation of the total congestion and its two shares is straightforward. So the procedure can help to set targets for, and to monitor the effectiveness of, both ramp-metering and demand-diversion policies.

Recurrent congestion fluctuates every day. So it is difficult empirically to calculate the additional delay caused by an incident during recurrent congestion. The procedure described here allows the calculation of the probability distributions of recurrent congestion, with and without incidents, provided incident data are available. In principle, the two distributions would tell us how much congestion is non-recurrent.

PeMS collects 30-sec, loop-detector data from California freeways. These data are analyzed in real-time and stored in the PeMS database. Many applications of interest to Caltrans management, engineers, planners, and the public are accessible over the World Wide Web at http://transacct.eecs.berkeley.edu. Other applications, like the one reported here, require direct access to the PeMS database.
2 Congestion delay and its components

Freeway congestion typically starts in a “chokepoint” link when flow into the link exceeds its revealed capacity. Density builds up in the chokepoint, and congestion infects upstream links, one by one. Recovery typically proceeds in the reverse direction. Demand first drops below revealed capacity in the most upstream congested links, and they become uncongested. The reduced demand propagates downstream, relieving links one by one.

Figure 1 shows the contour plots of a section of I-405N, extending from postmile 0 to 7, during the time interval 5.00-10.00 am, for 22 weekdays in June, 1998. For each contour plot, the x-axis is time, the y-axis is distance (vehicles travel from bottom to top). Darker points correspond to lower speeds.

There is free flow at 5.00 am, with vehicles traveling at 60 mph. The morning commute congestion starts shortly before 7.00 am near postmile 5. The contagion spreads upstream. At the depth of the congestion speed is below 15 mph. Demand eventually falls sufficiently to bring relief to the most upstream links of the congested region, and relief propagates downstream. Most days, free flow is restored by 9.30 am. Although there is congestion every morning, the contour plots also reveal daily fluctuations.

We analyze the congestion on the morning of June 1, 1998. Figure 2 shows three graphs. The top graph is the time (in vehicle-hours-traveled or VHT) that vehicles actually spent on this section in each 5-minute time interval between 5.00 and 10.00 am. The middle graph is the VHT they would have spent in each 5-minute interval under ideal metering that maintains maximum flow at free flow speed of 60 mph on the freeway. (Ideal metering is described later.) Under ideal metering, some vehicles would spend time at the ramps, and the middle graph includes that time. The bottom graph is the time that vehicles would spend traveling in the study section under free flow conditions (60 mph). So the bottom graph is the same as the middle graph, excluding time spent at the ramps.

The area under the top graph is the actual total VHT spent on this section of I-405N on June 1, 1998 between 5.00-10.00 am. The area under the bottom graph is the total time they would have spent traveling at 60 mph. The difference between the two areas is the total congestion delay, $\text{Delay}_{\text{tot}}$.

Define

\[
\begin{align*}
\text{Delay}_{\text{tot}} &= \text{Area under top graph} - \text{Area under bottom graph}, \\
\text{Delay}_{\text{met}} &= \text{Area under top graph} - \text{Area under middle graph}, \\
\text{Delay}_{\text{dem}} &= \text{Area under middle graph} - \text{Area under bottom graph}.
\end{align*}
\]

The total delay can be divided into two parts,

\[
\text{Delay}_{\text{tot}} = \text{Delay}_{\text{met}} + \text{Delay}_{\text{dem}}.
\]

$\text{Delay}_{\text{tot}}$ is the congestion delay—the extra time spent traveling below 60 mph. $\text{Delay}_{\text{met}}$ is the delay that can be eliminated by ideal metering. $\text{Delay}_{\text{dem}}$ is the delay due to excess demand (demand larger than revealed capacity); it can only be avoided by shifting demand.
### Table 1: \( Delay_{\text{tot}} \) and the delay remaining after ideal metering \( Delay_{\text{met}} \) for 10 days in June 1998.

<table>
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<th>704</th>
<th>534</th>
<th>808</th>
<th>353</th>
<th>340</th>
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<th>595</th>
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<td>( Delay_{\text{tot}} )</td>
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<tr>
<td>( Delay_{\text{met}} )</td>
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<td>446</td>
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<td>209</td>
<td>247</td>
<td>550</td>
<td>138</td>
<td>1266</td>
<td>87</td>
</tr>
</tbody>
</table>

An eyeball estimate from figure 2 gives

\[
Delay_{\text{tot}} = 500 \text{ VHT}, \quad Delay_{\text{met}} = 350 \text{ VHT}, \quad Delay_{\text{dem}} = 150 \text{ VHT}.
\]

So on June 1, 1998, out of the total congestion delay of 500 VHT, 350 VHT could, in principle, be eliminated by ramp metering. The remaining 150 VHT of delay is due to demand in excess of the capacity of this freeway section. It can only be avoided by diverting demand, perhaps by telling motorists how much time they would spend parked at the ramps.

Table 1 gives estimates of these delays for 10 different days in June 1998. On average, about two-thirds of the total congestion delay could be eliminated by ideal metering. Of course, in other freeway sections, the delay shares may be different.

The remainder of the paper explains the underlying concepts and the procedure used to obtain these delays using PeMS loop detector data.

## 3 Revealed capacity

The PeMS procedure relies on the concept of the **revealed capacity** of a link. We develop this concept in the context of the I-405N study section during the congestion episode on June 1, 1998, 5:00-10:00 am. The study section is depicted in figure 3. The figure shows the location of the detectors on the mainline and on the ramps.

Each link has four or five lanes and one HoV lane. There are 13 links and eight on- and off-ramps. The first on-ramp is virtual, representing metering of traffic upstream of the study section, presumably implemented by ramps there. A **link** is a portion of freeway associated with the loops at one location and extending half way to the next upstream and downstream loops, as in figure 4. A link may contain at most one on- or off-ramp. The links in the study section are named ML1, · · · , ML13 (ML denotes mainline detectors).

The top left graph in figures 6–18 plots the actual flow in vehicles per hour (VPH) vs occupancy (percent) for the 13 links ML1–ML13. (Ignore for now the other three plots in the figures.) Initially vehicles travel at 60 mph.\(^1\) Flow increases until it reaches a maximum value and congestion starts. Speed and flow now drop while occupancy increases. Eventually demand drops and speed gradually increases until the free flow regime is recovered.

In all cases the plots looks like that shown in figure 5. We have examined flow vs occupancy in hundreds of links in Los Angeles and Orange Counties. They all behave like the figure. We conclude that in California, maximum throughput occurs at the freeflow speed of 60 mph. Hence

\(^1\)The slopes of the initial straightline portion in the plots all correspond to a speed of 60 mph.
Congestion delay should be measured as the additional vehicles hours traveled driving below 60 mph.

We define the **revealed capacity of a link** to be the maximum sustainable flow in VPH that is reached in that link. PeMS data are used to calculate the revealed capacity of the 13 links in the study section during the congestion episode. From the flow vs occupancy plots we find that the maximum flow for ML1 and hence its capacity is 9,300 VPH, the capacity of ML2 is 10,000 VPH, the capacity of ML3 is 10,000 VPH, and so on. In this way we obtain the revealed capacity $C_k$ for every link $k$.

Revealed capacity is thus an empirical concept and its measurement will vary from day to day. But if the concept is sound, the revealed capacity numbers should be close to each other during recurrent congestion episodes.² And that is indeed the case. Figure 27 plots the PeMS capacity numbers for the 13 links in the study section for five days in June 1998 during the recurrent congestion of the morning commute.

The remarkable agreement in the capacity calculations for different days for each of the 13 links lends credence to the proposition that the revealed capacity is a stable characteristic of traffic behavior. But instead of being constant, it is more in accord with the data to regard revealed capacity as a *stochastic* quantity with a narrow range of daily variability.³

Observe that the capacities of the 13 links according to their physical characteristics are virtually the same (Figure 3), but their revealed capacities vary by as much as 50 percent, so predictions based on physical capacity can mislead. It is a challenge to traffic theory to explain the stability of the empirical measurement of revealed capacity and to determine the revealed capacity of a link from the network topology and traffic pattern.

## 4 Ideal metering and excess demand

The notion of revealed capacity suggests the following prediction about traffic behavior:

> If a metering policy keeps flow below its revealed capacity in every link throughout a congestion episode, the speed will be maintained at 60 mph, i.e. congestion will disappear. A consequence of the metering is that vehicles will be stopped at the ramps for some time.

We call this the **Ideal Metering Principle** (IMP). Of course we don’t know if IMP holds in practice, but the evidence lends it plausibility. The ideal metering policy is based on this principle. For on-ramp $r$, let $d(r)$ be the link downstream of $r$ (in figure 4 this is the link containing on-ramp $r$) and let $u(r)$ be the link upstream of $r$. Then in any period $t$, ramp $r$ should be metered at rate $On_r(t)$ equal to the downstream link capacity $C_{d(r)}$ minus the flow on the upstream link $u(r)$. If traffic

²Of course, if there are incidents or lane closures, the revealed capacity can be quite different.
³The variability may be due to microscopic shifts in driver behavior, traffic patterns, weather, etc. This belief is supported by an observation based on the figure—the capacities of all links move together, i.e. on some days they are all slightly larger or all slightly smaller. There is likely to be the same underlying cause.
behavior satisfies IMP, then under ideal metering, flow on all links will not exceed revealed capacity and traffic will move at 60 mph.

Queues may build up at ramps under ideal metering. We define excess demand delay as the queuing delay under ideal metering. This definition is appropriate because any attempt to reduce it by increasing the metering rate will lead to congestion and an increase in the total delay. The excess demand delay can only be reduced by shifting demand over time or to other modes. We now estimate this delay.

We use the following data from PeMS for every 5-minute interval $t$ from 5.00 to 10.00 am:

$$
\begin{align*}
In_r(t) & = \text{inflow into on-ramp } r \text{ in } t, \\
Out_s(t) & = \text{outflow into off-ramp } s \text{ in } t, \\
Vol_k(t) & = \text{flow on link ML}_k \text{ of study section in } t.
\end{align*}
$$

All these quantities are in VPH. The first two quantities characterize the exogenous demand during the congestion episode: how many vehicles enter each on-ramp $r$ and leave from each off-ramp $s$. Included in these are the virtual on-ramp upstream and off-ramp downstream of the study section.

We assume that the exogenous demand is unchanged by the metering policy.$^4$

The link flows will of course be changed by metering and we denote them by a superscript, e.g., $Vol^\text{met}_k(t)$ is the flow in link ML$_k$ in $t$. These flows are easy to calculate:$^5$

$$
Vol^\text{met}_k(t) = \text{Sum of metered flows } In^\text{met}_r(t) \text{ from all on-ramps } r \text{ upstream of ML}_k \\
- \text{Sum of outflows } Out_s(t) \text{ into all off-ramps } s \text{ upstream of ML}_k. \tag{2}
$$

The outflows $Out_s(t)$ are part of the data. The metered flows $In^\text{met}_r(t)$ are determined below in (5).

Next we calculate the queue build-up at each ramp. Consider on-ramp $r$, including the virtual ramp upstream of ML1. At time $t$ this ramp will have a queue of $q^\text{met}_r(t)$ vehicles given by

$$
q^\text{met}_r(t+1) = [q^\text{met}_r(t) + In_r(t) - On_r(t)]^+, \quad t = 0, 1, \cdots \tag{3}
$$

Here,

$$
On_r(t) = C_{d(r)} - Vol^\text{met}_{u(r)}(t) \tag{4}
$$

is the ideal metering rate of on-ramp $r$ in VPH, $In_r(t)$ is the demand in VPH at this ramp from PeMS data, and the notation $[x]^+ = \max\{x, 0\}$ guarantees that queues can’t be negative. The boundary

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$^4$Of course demand will increase in response to reduced travel times. So this assumption is just part of the “thought experiment” for calculating excess demand. The calculation could, in principle, be extended to incorporate a demand-response model.

$^5$Equation (2) takes this simple form because at 60 mph a vehicle traverses the entire section within one 5-minute period. If the study section was, say, 20 miles long, so that the free flow travel time would take four 5-minute periods, the outflows in $t$ would depend on the inflows at $t, t - 1, t - 2, t - 3, t - 4$ and the equation would be more complex.
condition of (3) is \( q_{r, \text{met}}(0) = 0 \), since initially (at 5.00 am) there is no congestion and hence no queue.

Under the metering policy, the metered inflow from ramp \( r \) is given by

\[
I_{r, \text{met}}(t) = \begin{cases} 
O_{r}(t), & \text{if } q_{r}(t) > 0 \\
I_{r}(t), & \text{if } q_{r}(t) = 0
\end{cases}
\]  

(5)

That is, so long as there is a queue, inflow is at the metered rate \( O_{r}(t) \); if there is no queue, inflow is at the measured demand \( I_{r}(t) \).

Equations (2)–(5) determine what happens under ideal metering. Traffic in the freeway section under study moves at 60 mph. Queues build up when there is excess demand, and then dissipate according to (3). Knowing the queues at each \( t \), we can calculate the average waiting time at each ramp.

The bottom left plots in Figures 6–18 show the occupancy from PeMS data (dotted line) and the occupancy under the metering policy (solid line). Notice how metering “clips” the congestion-causing high-occupancy periods.

Since speed is a constant 60 mph under metering, occupancy is strictly proportional to flow \( V_{r, \text{met}}(t) \) as is seen by comparing with the bottom left and top right plots in Figures 6–18. Observe that occupancy is a much more sensitive measure of how close the flow is to revealed capacity. So, it is much better to implement the ideal metering policy (4) using measured occupancy downstream of the ramp rather than measured flow upstream of the ramp.

Figures 19–26 describe the queue behavior at the 8 on-ramps. In each case, the top left shows the demand \( I_{r}(t) \) (dotted line) and the metered inflow \( I_{r, \text{met}}(t) \) (solid line). Queues build up when \( I_{r}(t) > I_{r, \text{met}}(t) \) and recede when the inequality is reversed. The top right is a plot of the queue \( q_{r, \text{met}}(t) \) at each 5-minute interval \( t \), calculated according to (3). The bottom right and left plots give the total waiting time (in hours) and the per vehicle average waiting time (in minutes). These quantities are calculated assuming that the departure and arrivals of vehicles (top left) are uniformly distributed over each 5-minute interval.

At ramps 2, 4, 6, and 8, the maximum waiting time is between 4 and 6 minutes and the maximum queue sizes are also large (as many as 120 vehicles). The large queues occur when demand is at its peak and, in unmetered congestion, everyone would be spending an extra 5 minutes crawling at 13 mph on the freeway. In light of this, a maximum queue size of 120 at a ramp is remarkably small.

For suppose only 30 vehicles could be accommodated at that ramp. This means that 120 - 30 = 90
vehicles would have to be diverted away from that ramp, corresponding to less than 6 minutes of a 1,000 VPH ramp capacity. The diversion could be in time or in space or in mode.

The only calculation that remains is the one shown in Figure 2. That is now simple. The total number of VHT spent driving on the freeway section in period \( t \) is

\[
\sum_k V_{ohlk}^{net}(t) \times \frac{L_k}{60},
\]

where \( L_k \) is the length of link ML\( k \). This is the bottom graph of Figure 2. The middle graph is simply the sum of this and the waiting time at all the ramps.

## 5 Implications and caveats

The study presented above has implications for freeway performance measurement, planning, metering, and demand management. Some of the implications are more firmly supported than others.

### Freeway performance

Travelers experience freeway performance by the reliability of travel time. The latter could be estimated as a combination of mean and variance or the 70th or 90th percentile of the travel time distribution. To our knowledge, no agency calculates such distributions. PeMS does this routinely. Figure 28 shows the travel time distributions for a 78-mile trip beginning between 5 and 8 am on I-5N in Los Angeles for 20 weekdays in July 2000. An 80 percent confidence interval yields a travel time of between 60 and 105 minutes!

In the absence of travel time measurements, Caltrans uses congestion as a performance measure. It declares a link congested when speed drops below 35 mph for at least 15 minutes. The data presented here and a comprehensive study of data from 4,000 detectors in Los Angeles show conclusively that maximum flow occurs at 60 mph. So the only defensible measure for California is the one proposed here: congestion delay is the additional vehicle hours spent traveling below 60 mph. There is some support within Caltrans to adopt this measure.

Caltrans districts publish an annual congestion report, based on data from “floating” cars driven through 5-7 mile sections of freeways twice a year during congested periods \[5 \]. Since the variation in travel times is enormous as Figure 28 indicates, these twice-a-year samples are unreliable. With a real-time system like PeMS it is now possible to track congestion accurately to determine trends as well as instantaneous departures from the trend. For example, PeMS can deliver a real-time alert whenever recurrent congestion exceeds the trend plus, say, twice the standard deviation.

Transportation agencies often use Level of Service (LOS) as defined by the Highway Capacity Manual (HCM2000) \[1, Chapter 23\] as a freeway performance measure. HCM2000 gives a procedure to calculate the speed and density on a freeway link, given the demand. A table defines LOS as a function of speed or density and the free flow speed. At the heart of the procedure are hypothesized speed-flow curves. In these curves the maximum throughput occurs at speeds well below
free flow. For example, a link with a free flow speed of 62 mph supports a per lane flow of 1600 vehicles/hour at the free flow speed and a 50 percent larger maximum flow of 2400 vehicles/hour at 50 mph. Data from Los Angeles show that LOS and throughput calculated in this manner would be completely wrong since in every link maximum throughput occurs at 60 mph. For California at least, the HCM2000 speed-flow curves are invalid.

Capacity

The HCM formula defines the capacity of a link by its maximum throughput, which depends on the free flow speed through the above-mentioned speed-flow curves. The free flow speed itself may be either directly measured or determined using another formula that gives free flow speed as a function of the link’s physical characteristics. Call the capacity calculated in this manner the HCM capacity. The HCM recommends using HCM capacity for operational uses (LOS calculation), and for design and planning (answering questions like the number of lanes needed to accommodate a certain flow at a specified LOS).

But as we have seen there is little relation between a link’s maximum observed throughput—its revealed capacity—and the HCM capacity based on the link’s physical capacity. Since both operational and planning decisions should be based on what a link can actually carry, it is revealed capacity that should inform those decisions. Operational and planning decisions based on HCM capacity will usually be incorrect.

The study shows that revealed capacity is an empirically stable notion. It remains an outstanding open question to explain this stability, and to calculate revealed capacity on the basis of a link’s connection to other links, the pattern of traffic, as well as its physical characteristics.

Lastly, revealed capacity is achievable under the ideal metering policy defined here. It is an important open question whether there are metering policies that can achieve sustained throughput that exceed revealed capacity.7

Ideal metering, excess demand, and system management

California freeway data support the idealized link behavior depicted in Figure 5. That behavior shows three regimes: until revealed capacity is reached traffic is at free flow; beyond that lies congestion—the regime of decreasing speed and increasing density; finally, the recovery phase is reached when demand drops well below revealed capacity.

The objective of ramp metering must be to achieve maximum flow and prevent the onset of congestion. The ideal ramp metering scheme is a local feedback rule that keeps occupancy downstream of each ramp below a critical level. Such local feedback rules are well-understood [4]. The point made here is that the best critical level is where the flow reaches revealed capacity.8

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7This observation is due to Markos Papageorgiou. A close study of Figures 6-18 shows that in many links throughput increases by between 2 and 5 percent for a period of 5 minutes, just before congestion sets in. Can this increased throughput be sustained by appropriate ramp metering?

8The ideal local feedback rule will perform better than the sophisticated system-wide adaptive controls of the SWARM
A practical ramp metering scheme must of course be more elaborate. The revealed capacity will change over the course of the day (afternoon and morning commute hours) and week (weekends vs weekdays), and it will be affected by the weather. The critical level must correspondingly change. Second, the metering scheme must react to unanticipated changes, such as incidents or lane closures. Third, once a ramp metering scheme is in place, travelers will react to it, changing the pattern of demand and, as a consequence, the revealed capacity might change. There should be a way to track these changes.

The ideal ramp metering scheme will lead to queues. When the queue at a ramp (Figures 19–26) becomes larger than can be accommodated there will be a spillover to city streets, provoking the ire of local citizens. Transportation officials deem such situations unacceptable, and ‘advanced’ metering schemes have over-rides that increase metering rates when queues become large. This, of course, is self-defeating as the resulting congestion will simply convert the nearby freeway into a parking lot, and the total delay will be much larger.

Suppose that the ramps in the study section can accommodate 30 vehicles. Then on-ramps 2, 4, 6, and 8 with maximum queue lengths of 170, 80, 120, and 40, respectively, will experience spillovers. Under ideal ramp metering the total number of vehicles that spill over during the entire congestion episode is the difference between the maximum queue length and the ramp capacity of 30, i.e. $140 + 50 + 90 + 10 = 290$ vehicles, amounting to less than 2 minutes of aggregate peak demand of 10,000 VPH. So instead of queue overrides, a more appropriate response is to divert traffic, through other means, including education. The procedures illustrated here can be used to calculate how much total delay is reduced at the cost of additional delay at the ramps. Moreover, changeable message signs that post ramp delays will encourage route divergence and relieve city streets.

The preceding two paragraphs underscore arguments for corridor-wide traffic management that coordinates the operation of ramp meters, arterial signals, changeable message signs, and other means of traffic control.

The calculations of the reductions in delay from metering and excess demand can be the starting point for the rational operation of a regional transportation system, because the calculations reveal the fundamental tradeoffs between freeway delay, queuing delay, and the distribution of demand over time and modes. Thus it is easy to answer questions like: how much diversion of demand originating at ramps in a given municipality is required to prevent spilling into city streets of queues at those ramps, or, how much additional delay will be caused if the traffic increased by, say, 5 percent. A quantitative evaluation of these tradeoffs can help assess the effectiveness of different transportation options: additional ramp storage capacity, an extra lane on a link, transit improvement, providing traveler information, etc.

Many California freeways have a HoV (High-occupancy Vehicle) lane on which one can legally drive a vehicle during congestion periods provided it carries at least two or three persons. HoV lanes enjoy free flow conditions during congestion. But usually the flow (in VPH, not in persons per hour) is below maximum throughput. If perfect metering is implemented, all lanes would experience free flow, and the use of HoV lanes would become problematic.
Measuring non-recurrent congestion

This important topic is only briefly discussed here. A more extended discussion will be presented in the future, following serious empirical study.

Non-recurrent congestion is supposed to account for a significant proportion of delays and additional accidents. But these claims lack empirical basis. The first difficulty is that recurrent congestion is a random quantity, varying from one day to the next (see Table 1); non-recurrent congestion is even more random. Furthermore, recurrent and non-recurrent congestion sometimes occur together. Thus it is very difficult to separate out the contributions of the two causes of congestion. The PeMS system, when it is augmented with incident and lane-closure data, will take care of the second difficulty.

The congestion measure proposed here can address the first difficulty. Consider again the study section and the morning congestion. We know the statistical distribution of the recurrent congestion. If there is an incident in this section during this period, PeMS can calculate the total congestion (the result of both recurrent and non-recurrent congestion). If congestion data for many incidents are available, we would create a statistical distribution of this total congestion. Comparing it with the distribution of the incident-free recurrent congestion will reliably estimate the contribution of incidents.

6 Conclusions

Freeway operational and planning decisions today rely on theories and practices exemplified, for example, by the Highway Capacity Manual, and simulation packages like Corsim or Paramics. PeMS studies show that these theories and practices are based on crucial hypothesized relationships—between speed and flow, and between a link’s capacity and its physical characteristics—that are in fact wrong. With access to large data sets provided by PeMS, the work needed to calibrate simulation models can be automated to a considerable extent. Simulation will then become an invaluable tool for both real-time operations and long-term planning studies.

PeMS is a large-scale freeway data collection, storage, and analysis project. It provides real-time and historical information of use to managers, engineers, planners, researchers, and travelers. It is inexpensive, easy to maintain, and can be readily duplicated in other states. PeMS makes available information based on masses of empirical data that can be used to create a reliable freeway traffic theory, a trustworthy practice of traffic engineering, and well-informed public transportation policy choices.

References

*See the careful I-880 Freeway Service Patrol study [5].

PeMS is now collecting incident data published by the California Highway Patrol. These data are not yet integrated with the loop-detector data.
REFERENCES


Figure 1: Contour plot of speed for a section of I-405N, for 22 weekdays in June 1998. The x-axis is time, from 5.00 to 10.00 am; the y-axis is distance from postmile 0 to 8. Vehicles travel from bottom to top. Darker points correspond to lower speed. The chokepoint link is near postmile 5.

7 Figures
Figure 2: The top graph is the amount of time in VPH actually spent on the freeway section, every 5 minutes. The units are normalized to VPH per hour, so the total vehicle-hours spent on this section, between 5.00 and 10.00 am is the area under the top graph. The middle graph is the time that would be spent under ideal metering, including time on the ramps. The bottom graph excludes time spent on the ramps, so it is the time that would be spent traveling at 60 mph.
Figure 3: The freeway study section has eight on and off-ramps.
Figure 4: A link is a portion of freeway associated with a set of loops, and may contain one on- or off-ramp. The link is indexed by the VDS ID of the loops.

Figure 5: Typical link behavior during a congestion episode. Vehicles travel at 60 mph until flow reaches capacity. Congestion starts. Speed and flow drop, occupancy increases to a maximum value. Demand then drops and speed gradually increases.
Figure 6: Performance of links ML1: actual and ideal metering.
Figure 7: Performance of links ML2: actual and ideal metering.
Figure 8: Performance of links ML3: actual and ideal metering.
Figure 9: Performance of links ML4: actual and ideal metering.
Figure 10: Performance of links ML5: actual and ideal metering.
Figure 11: Performance of links ML6: actual and ideal metering.
Figure 12: Performance of links ML7: actual and ideal metering.
Figure 13: Performance of links ML8: actual and ideal metering.
Figure 14: Performance of links ML9: actual and ideal metering.
Figure 15: Performance of links ML10: actual and ideal metering.
Figure 16: Performance of links ML11: actual and ideal metering.
Figure 17: Performance of links ML12: actual and ideal metering.
Figure 18: Performance of links ML13: actual and ideal metering.
Figure 19: Queue behavior at on-ramp 1 under metering.
Figure 20: Queue behavior at on-ramp 2 under metering.
Figure 21: Queue behavior at on-ramp 3 under metering.
Figure 22: Queue behavior at on-ramp 4 under metering.
Figure 23: Queue behavior at on-ramp 5 under metering.
Figure 24: Queue behavior at on-ramp 6 under metering.
Figure 25: Queue behavior at on-ramp 7 under metering.
Figure 26: Queue behavior at on-ramp 8 under metering.
Figure 27: The PeMS capacity calculations for the links in the study section for five days in June 1998. The close agreement lends credence to the PeMS capacity definition.

Figure 28: The travel time distribution for a 78-mile trip on I-5N in Los Angeles during weekdays in July 2000.